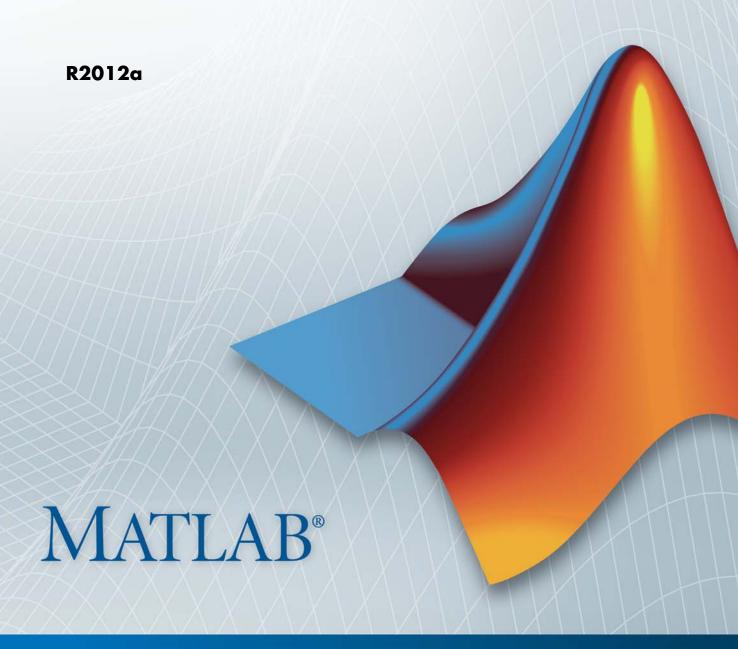
Phased Array System Toolbox™

Getting Started Guide





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Phased Array System Toolbox™ Getting Started Guide

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|----------------|-------------|----------------------------------|
| September 2011 | Online only | Revised for Version 1.1 (R2011b) |
| March 2012 | Online only | Revised for Version 1.2 (R2012a) |

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Getting Started with Phased Array System Toolbox Software

- "Product Description" on page 1-2
- "Limitations" on page 1-4
- "Standards and Conventions" on page 1-5

Product Description

Design and simulate phased array signal processing systems

Phased Array System ToolboxTM provides algorithms and tools for the design, simulation, and analysis of phased array signal processing systems. These capabilities are provided as MATLAB® functions and MATLAB System objects. The system toolbox includes algorithms for waveform generation, beamforming, direction of arrival estimation, target detection, and space-time adaptive processing.

The system toolbox lets you build monostatic, bistatic, and multistatic architectures for a variety of array geometries. You can model these architectures on stationary or moving platforms. Array analysis and visualization tools help you evaluate spatial, spectral, and temporal performance. The system toolbox lets you model an end-to-end phased array system or use individual algorithms to process acquired data.

Key Features

- Algorithms available as MATLAB functions and MATLAB System objects
- Monostatic, bistatic, and multistatic phased array system modeling
- Array analysis and 3D visualization; physical array modeling for uniform linear arrays, uniform rectangular arrays, and arbitrary conformal arrays on platforms with motion
- Broadband and narrowband digital beam-forming functions, including MVDR/Capon, LCMV, time delay, Frost, time delay LCMV, and subband phase shift
- Space-time adaptive processing algorithms, including displaced phase center array (DPCA), adaptive DPCA, sample matrix inversion (SMI), and angle-Doppler response visualization
- Direction of arrival algorithms, including MVDR, ESPRIT, beamscan, root MUSIC, and monopulse
- Waveform synthesis functions for pulsed CW, linear FM, stepped FM, and staggered PRF signals, and waveform visualization tools for ambiguity function and matched filter response

• Algorithms for TVG, pulse compression, coherent and noncoherent integration, CFAR processing, plotting ROC curves, and estimating range and Doppler

Limitations

In this section...

"MATLAB® Compiler™ Support" on page 1-4

"Code Generation Support" on page 1-4

MATLAB Compiler Support

Phased Array System Toolbox software does not support the MATLAB CompilerTM. You cannot compile any functionality in the toolbox.

Code Generation Support

Phased Array System Toolbox software does not support automatic generation of C code. You cannot generate code from the functions or System objects in the toolbox.

Standards and Conventions

In this section...

"Scope of Standards and Conventions" on page 1-5

"Complex-Valued Baseband Signals" on page 1-5

"Data Organization of Baseband Signals" on page 1-6

"Spatial Coordinates" on page 1-6

"Physical Quantities" on page 1-6

"Supported Data Types" on page 1-6

Scope of Standards and Conventions

Phased Array System Toolbox software uses consistent conventions with respect to units of measure, data representations, and coordinate systems. You must understand these conventions to use the toolbox.

Complex-Valued Baseband Signals

In phased array signal processing, it is common to shift the frequency content of a waveform to support effective radiation and propagation in the medium. You accomplish this task by modulating a baseband signal with nonzero spectral magnitudes in the vicinity of zero frequency to create a bandpass signal with nonzero spectral magnitudes centered around a carrier frequency. Typically, the bandwidth of the baseband signal is small compared to the carrier frequency resulting in a narrowband signal. To process returned signals, the receiver demodulates the bandpass signal to the baseband. The demodulation involves local oscillators both in phase and 90 degrees out of phase with the modulating carrier frequency. This demodulation results in in-phase (I) and quadrature (Q) baseband signals, or channels. For processing, it is convenient to create a complex-valued baseband signal by assigning the I channel to be the real part and the Q channel to be the imaginary part, I+jQ.

This software uses the complex-valued baseband representation to represent both transmitted and received signals. Actual phased array systems transmit real-valued signals and create complex-valued baseband signals only at the receiver. However, you can use a complex-valued representation at all stages. Doing so enables you to accurately model the effect of system gains, losses, and interference on the received signal samples.

Data Organization of Baseband Signals

You can use this software to efficiently implement space-time processing of complex-valued baseband samples by organizing the data in a three-dimensional matrix. See Radar Data Cube for an explanation of how the software organizes space-time data.

Spatial Coordinates

Representation of position in three dimensions is a fundamental aspect of array signal processing. This software specifies rectangular and spherical coordinates as column vectors with respect to both global and local origins. See "Coordinate Systems and Motion Modeling" for a detailed explanation of the conventions.

Physical Quantities

This software uses the International System of Units (SI) almost exclusively for measurement. In addition, there are physical constants declared and used in calculations. See "Units of Measure and Physical Constants" on page 3-7 for a detailed explanation of the conventions.

Supported Data Types

This software supports only double-precision data types.

Phased Array Systems

System Overviews

In this section...

"Phased Array System Overview" on page 2-2

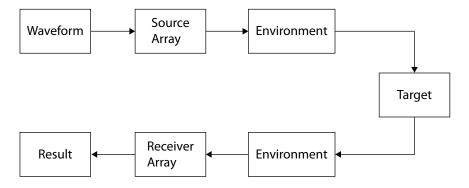
"Phased Array Radar Overview" on page 2-4

Phased Array System Overview

Phased array systems use the spatial and temporal characteristics of propagating space-time wavefields to extract information about any sources of the wavefields. By processing data collected over a spatiotemporal aperture using an array of sensors, you can significantly improve performance over a single sensor in a number of areas. These areas include, but are not limited to:

- Signal detectability
- Spatial selectivity
- Source identification and localization

The following figure shows a high-level overview of a phased array system.



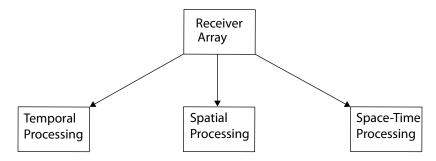
Phased array systems in diverse applications, such as radar, sonar, medical ultrasonography, medical imaging, and cellular phone communication share many common elements including:

• **Source Array** — The source array transmits a waveform through an environment. The waveform often consists of repeating pulses modulated

by a carrier frequency. Depending on the application, the wave may be an acoustic (mechanical), or electromagnetic wave. The source array is often electronically or mechanically steered to transmit in preferred directions.

- **Environment** The medium in which the waveform travels to and from the target affects a number of system parameters including propagation speed, absorption loss, and wave dispersion.
- **Target** The target reflects a portion of the incident waveform energy from the source array. Some percentage of the reflected energy is backscattered in the direction of the receiver array. In some applications, the target is the source of the waveform energy.
- **Receiver Array** The receiver array collects energy from the target representing the *signal* along with external and internal sources of *noise*. The receiver implements algorithms to improve the signal-to-noise ratio and extract space-time information from the signal.

At the receiver, phased array systems implement algorithms to extract temporal and spatial information about the source, or sources of energy. The following figure shows a high-level overview of array signal processing algorithms common to a significant number of phased array systems.



Brief descriptions of the three categories are:

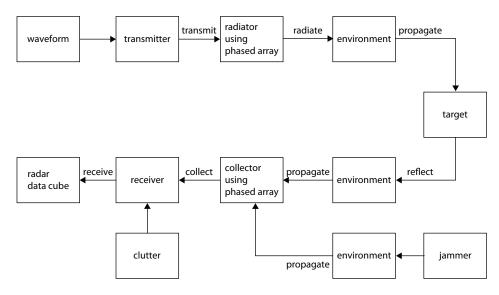
• **Temporal Processing** — Phased arrays often operate in poor signal-to-noise (SNR) ratios. Employing temporal integration and matched filtering improves the SNR. Knowing the propagation speed of the transmitted waveform and measuring the time it takes for a pulse to travel to and from a target allows phased array systems to estimate range.

Performing Fourier analysis on a time series of pulses enables the phased array to extract Doppler information from moving targets.

- Spatial Processing Combining weighted information across multiple sensor elements with a known geometry enables phased array systems to spatially filter incoming waveforms. Phased arrays can also estimate the direction of arrival and the number of source waveforms incident on the array.
- **Space-Time Processing** Simultaneously analyzing both spatial and temporal information enables phased array systems to produce joint angle-Doppler measurements of incident waveforms. Space-time processing enables phased array systems to distinguish moving targets from stationary targets when the phased array is in motion.

Phased Array Radar Overview

The following figure presents an overview of a radar phased array system. The figure expands on the high-level overview shown in "Phased Array System Overview" on page 2-2.



To exploit the advantages of array processing, you must first understand how to model and optimize the performance of each component and operation in a phased array system. This software provides models for all the components of the phased array system illustrated in the preceding figure from signal synthesis to signal analysis.

The software supports models in which the transmitter and receiver are collocated or spatially separated. The software also supports models in which both the targets and phased array are in motion.

Waveform Synthesis

Phased Array System Toolbox software supports the design of rectangular, linear frequency-modulated, and linear stepped-frequency pulsed waveforms. To create such waveforms, you use phased.RectangularWaveform, phased.LinearFMWaveform, and phased.SteppedFMWaveform.

Physical Components and Environment Modeling

The software enables you to simulate the physical components of a phased array system, including:

- **Transmitter** You can specify the transmitter peak power, gain, and loss factor. See phased. Transmitter for details.
- Antenna elements You can create antenna elements with isotropic response patterns or antenna elements with user-specified response patterns. These response patterns can encompass the entire range of azimuth ([-180,180] degrees) and elevation ([-90,90] degrees) angles. See phased.IsotropicAntennaElement, phased.CosineAntennaElement, and phased.CustomAntennaElement for details.
- Microphone elements For acoustic applications, you can model an omnidirectional or custom microphone with phased.OmnidirectionalMicrophoneElement or phased.CustomMicrophoneElement.

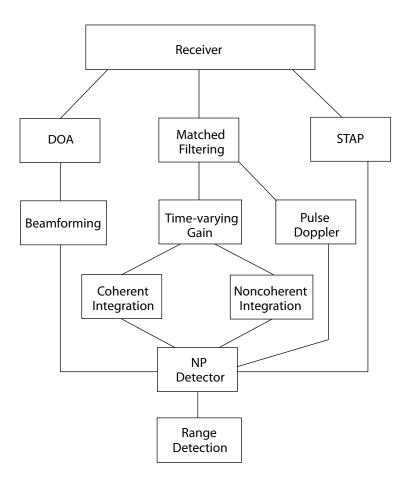
Phased arrays — There are System objects for three phased array geometries:

Uniform linear array (ULA) — phased.ULA enables you to model a
uniform linear array consisting of sensor elements with isotropic or
custom radiation patterns. You can specify the number of elements and
element spacing.

- Uniform rectangular array phased. URA enables you to model a uniform rectangular array of sensor elements with isotropic or custom radiation patterns. You can specify the number of elements, element spacing along two orthogonal axes, and lattice geometry.
- Conformal array phased.ConformalArray enables you to model a conformal array of sensor elements with isotropic or custom radiation patterns. To do so, specify the antenna element positions and normal directions.
- **Radiator** You can model waveform radiation through an antenna element, microphone, or array with the phased.Radiator object.
- **Environment** You can model the propagation of an electromagnetic (EM) wave in free space with phased.FreeSpace. You can simulate one-way or two-way propagation of a narrowband EM signal by applying range-dependent attenuation and time delays, or phase shifts.
- Target You can simulate a target with a specified radar cross section (RCS) using phased.RadarTarget. phased.RadarTarget supports both nonfluctuating and fluctuating (random) models of the RCS. The toolbox supports a family of random models based on the chi-square distribution known as *Swerling target models*.
- **Interference** You can simulate wideband interference with a user-specified radiated power, using phased.BarrageJammer.
- Clutter You can simulate surface clutter using phased.ConstantGammaClutter.
- Signal collection You can simulate far-field or near-field narrowband and wideband signal reception from specified directions using phased.Collector and phased.WidebandCollector.
- Receiver phased.ReceiverPreamp enables you to simulate the gain, loss factor, and internal noise characteristics of your receiver.

Array Signal Processing

For the processing of received data, Phased Array System Toolbox software supports a wide-range of array signal processing algorithms. The following figure presents a more detailed view of the general concepts discussed in "Phased Array System Overview" on page 2-2.



The preceding figure only presents an overview of the array signal processing operations supported by the software rather than predetermined orders of operation. For example, direction of arrival (DOA) estimation, beamforming, and space-time adaptive processing (STAP) often follow operations that improve the signal-to-noise ratio such as matched filtering. You can implement the supported algorithms in the manner best-suited to your application.

• **Matched Filtering** — You can perform matched filtering on your data with phased.MatchedFilter. See "Matched Filtering" for examples.

- Time-varying gain You can equalize the power level of the incident waveform across samples from different ranges using phased.TimeVaryingGain. This object compensates for signal power loss due to range.
- Beamforming and direction-of-arrival (DOA) estimation The Phased Array System Toolbox provides a number of algorithms for beamforming and direction of arrival estimation. See "Beamformers" and "Direction of Arrival (DOA)" for a list of supported beamforming and DOA algorithms. You can find example workflows for each in "Beamforming" and Direction of Arrival (DOA) Estimation.
- **Detection** A number of utility functions implement and evaluate Neyman-Pearson detectors using both coherent and noncoherent pulse integration.

The toolbox also provides routines for evaluating detector performance through the construction of receiver operating characteristic curves.

To model fluctuating noise characteristics, phased.CFARDetector object adaptively estimates the noise characteristics from the data to maintain a constant false-alarm rate.

You can find example workflows in the "Detection" section of the User's Guide.

• Pulse Doppler — The Phased Array System Toolbox has utility functions for estimating Doppler shift based on speed (speed2dop) and to estimate speed based on the Doppler shift (dop2speed. You can implement pulse-Doppler processing by using the spectrum estimation algorithms in the Signal Processing ToolboxTM product on the slow-time data. See "Radar Data Cube" on page 3-2 for an explanation of the slow-time data.

See "Doppler Shift and Pulse-Doppler Processing" for examples of Doppler processing.

To calculate the joint angle-Doppler response of the input data, use phased.AngleDopplerResponse.

Example workflows for computing the angle-Doppler response can be found in "Angle-Doppler Response".

• Space-time adaptive processing — You can implement displaced phase center antenna techniques with phased.DPCACanceller and phased.ADPCACanceller.phased.STAPSMIBeamformer implements an

adaptive beamformer by calculating the beamformer weights using the estimated space-time interference covariance matrix.

See "Space-Time Adaptive Processing (STAP)" for examples.

Radar Data Cube, Units, and Physical Constants

- "Radar Data Cube" on page 3-2
- "Units of Measure and Physical Constants" on page 3-7

Radar Data Cube

In this section...

"Radar Data Cube Concept" on page 3-2

"Fast Time Samples" on page 3-3

"Slow Time Samples" on page 3-4

"Spatial Sampling" on page 3-4

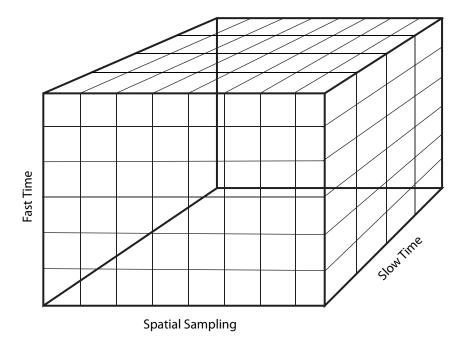
"Space-Time Processing" on page 3-5

"Organizing Data in the Radar Data Cube" on page 3-5

Radar Data Cube Concept

The radar data cube is a convenient way to conceptually represent space-time processing. To construct the radar data cube, assume that preprocessing converts the RF signals received from multiple pulses across multiple array elements to complex-valued baseband samples. Arrange the complex-valued baseband samples in a three-dimensional array of size *M*-by-*N*-by-*L*. Many radar signal processing operations in Phased Array System Toolbox software correspond to processing lower-dimensional subsets of the radar data cube. The subset could be a one-dimensional subvector or a two-dimensional submatrix.

The following figure shows the organization of the radar data cube in this software. Subsequent sections explain each of the dimensions and which aspect of space-time processing they represent.



Fast Time Samples

Consider each *M*-by-1 subvector of the radar data cube. Each of these *M*-by-1 column vectors represent complex-valued baseband samples from one pulse at one array element. Because pulse bandwidths can be on the order of a few hundred kHz, you require high sampling rates to avoid aliasing. Such high sampling rates lead to the designation *fast time*.

The fast time dimension is also referred to as the *range* dimension. If the two-way range to a target from the phased array is 2R, the difference in range, ΔR , represented by two samples acquired with sampling interval, T is:

$$\Delta R = \frac{cT}{2}$$

Each sample in the fast time dimension represents an incremental change in range of ΔR in range. For this reason, fast time samples are also referred to as *range bins*, or *range gates*.

Pulse compression is an example of a signal processing operation performed on the fast time samples.

Slow Time Samples

Consider each M-by-L submatrix of the radar data cube. In the submatrix there are M row vectors with dimension 1-by-L. Each of these row vectors contains complex-valued baseband samples from L different pulses corresponding to the same range bin. There is a M-by-L matrix for each of the N array elements. The sampling interval between the L samples is the pulse repetition interval (PRI). Typical PRIs are much longer than the fast-time sampling interval. Because of the long sampling intervals, samples taken across multiple pulses are referred to as $slow\ time$.

Processing data in the slow time dimension allows you to estimate the Doppler spectrum at a given range bin.

The Nyquist criterion applies equally to the slow-time dimension. The reciprocal of the PRI is the *pulse repetition frequency* (PRF). The PRF gives the width of the unambiguous Doppler spectrum.

Spatial Sampling

Phased arrays consist of multiple array elements. Consider each M-by-N submatrix of the radar data cube. Each column vector consists of M fast-time samples for a single pulse received at a single array element. The N column vectors represent the same pulse sampled across N array elements. The sampled data in the N column vectors is a spatial sampling of the incident waveform. Analysis of the data across the array elements allows you to examine the spatial frequency content of each received pulse.

It is also possible to spatially sample a wavefield by mechanically steering a single antenna, but the more common scenario is to sample the wavefield by multiple array elements. The Nyquist criterion for spatial sampling dictates that array elements must not be separated by more than one-half the wavelength of the carrier frequency.

Beamforming is a spatial filtering operation that combines data across the array elements to selectively enhance and suppress wavefields incident on the array from particular directions.

Space-Time Processing

Space-time adaptive processing operates on the two-dimensional angle-Doppler data for each range bin. Consider the M-by-N-by-L radar data cube. Each of the M samples is data from the same range. This range is sampled across N array elements, and L PRIs. Collapsing the three-dimensional matrix at each range bin into N-by-L submatrices allows the simultaneous two-dimensional analysis of angle of arrival and Doppler frequency.

Organizing Data in the Radar Data Cube

If you have M complex-valued baseband data samples collected from L pulses received at N sensors, you can organize your data in a format compatible with the Phased Array System Toolbox conventions using permute. After processing your data, you can convert back to your original data cube format with ipermute.

Reordering the Data Cube

Assume you have a data set consisting of 200 samples per pulse for ten pulses collected at 6 sensor elements. Assume that your data are organized as a 6-by-10-by-200 matrix. Simulate this data structure using complex-valued white Gaussian noise samples.

```
OrigData = randn(6,10,200)+1j*randn(6,10,200);
```

The first dimension of OrigData is the number of sensors (spatial sampling), the second dimension is the number of pulses (slow-time), and the third dimension contains the fast-time samples. This format is not compatible with the radar data cube conventions of the Phased Array System Toolbox.

The Phased Array System Toolbox expects the first dimension to contain the fast-time samples, the second dimension to represent individual sensors in the array, and the third dimension to contain the slow-time samples.

To reorganize OrigData in a format compatible with the toolbox conventions, enter:

```
NewData = permute(OrigData,[3 1 2]);
```

The preceding line of code moves the third dimension of OrigData to be the first dimension of NewData. The first dimension of OrigData becomes the second dimension of NewData and the second dimension of OrigData becomes the third dimension of NewData. This results in NewData being organized as fast-time samples-by-sensors-by-slow-time samples. You can now process NewData with the Phased Array System Toolbox software.

After you process your data, you can use ipermute to return your data format to the original structure.

```
Data = ipermute(NewData,[3 1 2]);
% Data is equal to OrigData
```

Units of Measure and Physical Constants

In this section...

"Units of Measure" on page 3-7

"Physical Constants" on page 3-7

Units of Measure

Phased Array System Toolbox software almost exclusively uses SI base and derived units to measure physical quantities. The software does not provide any utilities for converting SI base or derived units to other systems of measurement.

Angles

Angles are an exception to the use of SI base and derived units. All angles in Phased Array System Toolbox software are specified in degrees. See "Spherical Coordinates" for an explanation of the angles used in the software. There are two utility functions for converting angles from radians to degrees and degrees to radians: radtodeg and degtorad.

Decibels

To accurately model and simulate phased array systems, it is necessary to account for gains and losses in power incurred at various stages of processing. In Phased Array System Toolbox software, these gains and losses are specified in decibels (dB). Signal to noise ratios (SNRs) and the receiver noise figure are also expressed in dB. A power of *P* watts in dB is:

$$10\log_{10}(P)$$

There are two utility functions for converting between dB and power: db2pow and pow2db, and two utility functions for converting between magnitude and dB: db2mag and mag2db.

Physical Constants

Modeling and simulating phased array systems requires that you specify values for a number of physical constants. For example, the distribution of thermal noise power per unit bandwidth depends on the Boltzmann constant. To measure Doppler shift and range in radar, you have to specify a value for the speed of light. The following table summarizes the three physical constants specified in the toolbox. See physconst for additional information.

| Description | Value |
|--------------------------------------------------------|---------------------------------------------------------------------------------|
| The speed of light in a vacuum | 299,792,458 meters/second. Most commonly denoted by c . |
| The Boltzmann constant relating energy to temperature. | $1.38 \mathrm{x} 10^{-23}$ joules/degree kelvin. Most commonly denoted by k . |
| Mean radius of the Earth | 6,137,000 meters |

System Objects

- "Create System Objects" on page 4-2
- "Set Up System Objects" on page 4-4
- "Process Data using System Objects" on page 4-7
- "What are System Object Locking and Property Tunability?" on page 4-12
- "Find Help and Demos for System Objects" on page 4-14

Create System Objects

In this section...

"Create a System Object" on page 4-2

"Define a New System Object" on page 4-2

"Change a System Object Property" on page 4-3

"Run a System Object" on page 4-3

"Display Available System Objects" on page 4-3

System objects are MATLAB object-oriented implementations of algorithms. They extend MATLAB by enabling you to model dynamic systems represented by time-varying algorithms. System objects are well integrated into the MATLAB language, regardless of whether you are writing simple functions, working interactively in the command window, or creating large applications.

In contrast to MATLAB functions, System objects automatically manage state information, data indexing, and buffering, which is particularly useful for iterative computations or stream data processing. This enables efficient processing of long data sets.

Note System objects do not support sparse matrices.

Create a System Object

To use System objects, you must first create an object. For example,

H = phased.LinearFMWaveform;

Define a New System Object

You can define a System object to implement your algorithm. For information and examples, see "Define New System Objects".

Change a System Object Property

In general, you should set the object properties before you use the step method to run data through the object. To change the value of a property, use this format,

```
H.SweepBandwidth = 2e5; % Set the SweepBandwidth property
H.SweepDirection = 'Down' % Set the SweepDirection property
```

The property values of the linear FM pulse waveform object, H, are displayed.

Run a System Object

To execute a system object, use the step method.

```
Y = step(H);
```

The output data from the step method is stored in Y, which, in this case, is a vector of samples from the linear FM pulse waveform.

Display Available System Objects

To see a list of all the System objects for a particular package, type help phased. To display help for specific objects, properties, or methods, see "Find Help and Demos for System Objects" on page 4-14.

Set Up System Objects

In this section...

"Create a New System Object" on page 4-4

"Retrieve System Object Property Values" on page 4-4

"Set System Object Property Values" on page 4-4

Create a New System Object

You must create a System object before using it. You can create the object at the MATLAB command line or within a program file. Your command-line code and programs can pass MATLAB variables into and out of System objects.

For general information about working with MATLAB objects, see *Object-Oriented Programming* in the MATLAB user documentation.

Retrieve System Object Property Values

System objects have properties that configure the object. You use the default values or set each property to a specific value. The combination of a property and its value is referred to as a *Name-Value pair*. You can display the list of relevant property names and their current values for an object by using the object handle only, <handleName>. Some properties are relevant only when you set another property or properties to particular values. If a property is not relevant, it does not display.

To display a particular property value, use the handle of the created object followed by the property name: <handle>.

Example

This example retrieves and displays the PeakPower property value for the previously created Transmitter object:

H.PeakPower

Set System Object Property Values

You set the property values of a System object to model the desired algorithm.

Note When you use Name-Value pair syntax, the object sets property values in the order you list them. If you specify a dependent property value before its parent property, an error or warning may occur.

Set Properties for a New System Object

To set a property when you first create the object, use Name-Value pair syntax. For properties that allow a specific set of string values, you can use tab completion to select from a list of valid values.

```
H1 = phased.Transmitter('PeakPower',6000)
```

where

- H1 is the handle to the object
- phased is the package name.
- Transmitter is the object name.
- CoefficientsSource is the property name.
 - PeakPower is the property name.
- 6000 is the property value.

Set Properties for an Existing System Object

To set a property after you have created an object, use either of the following syntaxes:

```
H1.PeakPower = 6500
or
set(H1,'PeakPower',6500)
```

Use Value-Only Inputs

Some object properties have no useful default values or must be specified every time you create an object. For these properties, you can specify only

the value without specifying the corresponding property name. If you use value-only inputs, those inputs must be in a specific order, which is the same as the order in which the properties are displayed. Refer to the object reference page for details. For example,

```
hURA = phased.URA([2 3], 0.25);
```

specifies the Size property as [2 3] and the ElementSpacing property as 0.25.

Process Data using System Objects

In this section...

"What are System Object Methods?" on page 4-7

"The Step Method" on page 4-7

"Common Methods" on page 4-9

"Advantages of Using Methods" on page 4-10

What are System Object Methods?

After you create a System object, you use various object methods to process data or obtain information from or about the object. All methods that are applicable to an object are described in the reference pages for that object. System object method names begin with a lowercase letter and class and property names begin with an uppercase letter. The syntax for using methods is <method>(<handle>), such as step(H).

The Step Method

The step method is the key System object method. You use step to process data using the algorithm defined by that object. The step method performs other important tasks related to data processing, such as initialization and handling object states. Every System object has its own customized step method, which is described in detail on the step reference page for that object. For more information about the step method and other available methods, see the descriptions in "Common Methods" on page 4-9.

Calculate the Effect of Propagating a Signal in Free Space

This example uses two different step methods. The first step method is associated with the phased.LinearFMWaveform object and the second step method is associated with the phased.Freespace object.

Construct a linear FM waveform with a pulse duration of 50 microseconds, a sweep bandwidth of 100 kHz, an increasing instantaneous frequency, and a pulse repetition frequency (PRF) of 10 kHz..

hFM = phased.LinearFMWaveform('SampleRate',1e6,...

```
'PulseWidth',5e-5,'PRF',1e4,...
'SweepBandwidth',1e5,'SweepDirection','Up',...
'OutputFormat','Pulses','NumPulses',1);
```

Obtain the waveform using the step method. Note that the input to the step method is a handle to a phased.LinearFMWaveform object.

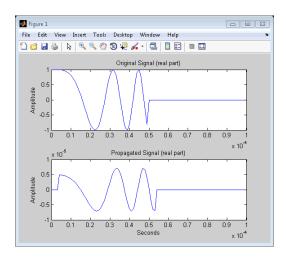
```
Sig = step(hFM);
```

Construct a free space object with a propagation speed equal to the speed of light, an operating frequency of 3 GHz, and a sample rate of 1 MHz. The free space object is constructed to model one way propagation.

```
hFS = phased.FreeSpace(...
    'PropagationSpeed',physconst('LightSpeed'),...
    'OperatingFrequency',3e9,'TwoWayPropagation',false,...
    'SampleRate',1e6);
```

Calculate the effect on the waveform of one-way propagation in free space from coordinates [0;0;0] to [500; 1e3; 20] and plot the results for comparison.

```
PropSig = step(hFS,Sig,[0; 0; 0],[500; 1e3; 20]);
% compare the original signal to the propagated waveform
t = unigrid(0,1/hFS.SampleRate,length(Sig)*1/hFS.SampleRate,'[)');
subplot(211)
plot(t,real(Sig)); title('Original Signal (real part)');
ylabel('Amplitude');
subplot(212)
plot(t,real(PropSig)); title('Propagated Signal (real part)');
xlabel('Seconds'); ylabel('Amplitude');
```



Common Methods

All System objects support the following methods, each of which is described in a method reference page associated with the particular object. In cases where a method is not applicable to a particular object, calling that method has no effect on the object.

| Method | Description |
|---------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| step | Processes data using the algorithm defined by the object. As part of this processing, it initializes needed resources, returns outputs, and updates the object states. After you call the step method, you cannot change any input specifications (i.e., dimensions, data type, complexity). During execution, you can change only tunable properties. The step method returns regular MATLAB variables. |
| | Example: $Y = step(H,X)$ |
| release | Releases any special resources allocated by the object, such as file handles and device drivers, and unlocks the object. See "Understand System Object Modes" on page 4-12. |
| clone | Creates another object with the same property values |

| Method | Description |
|------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| isLocked | Returns a logical value indicating whether the object is locked. See "Understand System Object Modes" on page 4-12. |
| reset | Resets the internal states of the object to the initial values for that object |
| isDone | Applies to source objects only. Returns a logical value indicating whether the step method has reached the end of the data file. If a particular object does not have end-of-data capability, this method value returns false. |
| info | Returns a structure containing characteristic information about the object. The fields of this structure vary depending on the object. If a particular object does not have characteristic information, the structure is empty. |
| getNumInputs | Returns the number of inputs (excluding the object itself) expected by the step method. This number varies for an object depending on whether any properties enable additional inputs. |
| getNumOutputs | Returns the number of outputs expected from the step method. This number varies for an object depending on whether any properties enable additional outputs. |
| getDiscreteState | Returns the discrete states of the object in a structure. If the object is unlocked (when the object is first created and before you have run the step method on it or after you have released the object), the states are empty. If the object has no discrete states, getDiscreteState returns an empty structure. |

Advantages of Using Methods

System objects use a minimum of two commands to process data—a constructor to create the object and the step method to run data through the object. This separation of declaration from execution lets you create multiple, persistent, reusable objects, each with different settings. Using this approach avoids repeated input validation and verification, allows for easy use within a programming loop, and improves overall performance. In contrast, MATLAB functions must validate parameters every time you call the function.

These advantages make System objects particularly well suited for processing streaming data, where segments of a continuous data stream are processed iteratively. This ability to process streaming data provides the advantage of not having to hold large amounts of data in memory. Use of streaming data also allows you to use simplified programs that use loops efficiently.

What are System Object Locking and Property Tunability?

In this section...

"Understand System Object Modes" on page 4-12

"Change Properties While Running System Objects" on page 4-13

"Change System Object Input Complexity or Dimensions" on page 4-13

Understand System Object Modes

System objects are in one of two modes: *unlocked* or *locked*. After you create an object and until it starts processing data, that object is in unlocked mode. You can change any of its properties as desired.

The object initializes and locks when it begins processing data. The typical way in which an object becomes locked is when the step method is called on that object. To determine if an object is locked, use the <code>isLocked</code> method. To unlock an object, use the <code>release</code> method. When the object is locked, you cannot change any of the following:

- Number of inputs or outputs
- Data type
- Dimensions of inputs or tunable properties, except for System objects that support variable-size data, where the input size can vary. See "What Is Variable-Size Data?" for more information.
- · Value of any nontunable property

Several System objects do not allow changing the complexity of inputs from real to complex. You can, however, change the input complexity from complex to real without unlocking the object.

These restrictions allow the object to maintain states and allocate memory appropriately.

Change Properties While Running System Objects

When an object is in locked mode, it is processing data and you can only change the values of properties that are *tunable*. To determine if a particular System object property is tunable, see the corresponding reference page or use a command of this form:

help phased.Transmitter.PeakPower

where

- phased is the package name.
- Transmitter is the object name.
- PeakPower is the property name.

For information on locked and unlocked modes, see "Understand System Object Modes" on page 4-12.

Change System Object Input Complexity or Dimensions

During simulations you can change an input's complexity from complex to real, but not from real to complex. You cannot change any input complexity during code generation.

For objects that do not support variable-size input, if you change the input dimensions while the object is in locked mode, the object produces a warning and unlocks. The object then reinitializes the next time you call the step method. See the object's reference page for more information. You can change the value of a tunable property and the input size without a warning or error being produced. For all other changes at runtime, an error occurs.

Find Help and Demos for System Objects

Refer to the following resources for more information about System objects.

- Package help help phased, where phased is a product package name
- Object help help phased. Transmitter, where Transmitter is the object name
- Documentation reference pages for an object doc phased. Transmitter
- Property help help phased.Transmitter.PeakPower, where PeakPower is the property name.
- Method help help phased. Transmitter. step, where step is the method name.

To view demos, go to the Help contents for the associated product.

Basic Radar Workflow

- "Overview of Basic Workflow" on page 5-2
- "End-to-End Radar System" on page 5-3

Overview of Basic Workflow

The scenario and code examples contained in "End-to-End Radar System" on page 5-3 are intended as an introduction to the fundamental workflow used in Phased Array System Toolbox software. The example is intentionally simplified in order to familiarize you with the basic theme that extends throughout the toolbox. You will find the core elements of this workflow in many other examples.

The basic workflow consists of:

- Constructing objects that represent the physical components and algorithms of your model. The objects have modifiable properties that enable you to parameterize your model. For information about the object properties, see the object reference page.
- Using the object's step method to perform the action of your parameterized object on inputs. The action of step is specific to each algorithm. For example, the step method for the linear FM waveform, phased.LinearFMWaveform, performs a different action than the step method for the steering vector, phased.SteeringVector. The specific action and syntax of each step method are documented on the reference page. You can access the documentation for an object's step method by entering:

doc phased.ObjectName/step

at the MATLAB command prompt, or via the hyperlink in the Methods section of the object's reference page.

End-to-End Radar System

In this section...

"Radar Scenario" on page 5-3

"Waveform" on page 5-3

"Antenna" on page 5-4

"Target Model" on page 5-4

"Antenna and Target Platforms" on page 5-4

"Modeling the Transmitter" on page 5-5

"Modeling Waveform Radiation and Collection" on page 5-6

"Modeling the Receiver" on page 5-6

"Modeling the Propagation Environment" on page 5-7

"Implementing the Basic Radar Model" on page 5-7

Radar Scenario

This example shows how to apply the basic toolbox workflow to the following scenario: Assume you have a single isotropic antenna operating at 4 GHz. Assume the antenna is located at the origin of your global coordinate system. There is a target with a nonfluctuating radar cross section of 0.5 square meters initially located at [7000; 5000; 0]. The target moves with a constant velocity vector of [-15;-10;0]. Your antenna transmits ten rectangular pulses with a duration of 1 microsecond at a pulse repetition frequency (PRF) of 5 kHz. The pulses propagate to the target, reflect off the target, propagate back to the antenna, and are collected by the antenna. The antenna operates in a monostatic mode, receiving only when the transmitter is inactive.

Waveform

To build the waveform described in "Radar Scenario" on page 5-3, use phased.RectangularWaveform and set the properties to the desired values.

```
hwav = phased.RectangularWaveform('PulseWidth',1e-6,...
'PRF',5e3,'OutputFormat','Pulses','NumPulses',1);
```

See "Rectangular Pulse Waveforms" for more detailed examples on building waveform models.

Antenna

To model the antenna described in "Radar Scenario" on page 5-3, use phased. Isotropic Antenna Element. Set the operating frequency range of the antenna to [1,10] GHz. The isotropic antenna radiates equal energy for azimuth angles from -180 to 180 degees and elevation angles from -90 to 90 degrees.

```
hant = phased.IsotropicAntennaElement('FrequencyRange',...
    [1e9 10e9]);
```

Target Model

To model the target described in "Radar Scenario" on page 5-3, use phased.RadarTarget. The target has a nonfluctuating RCS of 0.5 square meters and the waveform incident on the target has a carrier frequency of 4 GHz. The waveform reflecting off the target propagates at the speed of light. Parameterize this information in defining your target.

```
htgt = phased.RadarTarget('Model','Nonfluctuating',...
    'MeanRCS', 0.5, 'PropagationSpeed', physconst('LightSpeed'),...
    'OperatingFrequency',4e9);
```

Antenna and Target Platforms

To model the location and movement of the antenna and target in "Radar Scenario" on page 5-3, use phased.Platform.

The antenna is stationary in this scenario and is located at the origin of the global coordinate system. The target is initially located at [7000; 5000; 0] and moves with a constant velocity vector of [-15;-10;0].

```
htxplat = phased.Platform('InitialPosition',[0;0;0],...
    'Velocity',[0;0;0],'OrientationAxes',[1 0 0;0 1 0;0 0 1]);
htgtplat = phased.Platform('InitialPosition',[7000; 5000; 0],...
    'Velocity',[-15;-10;0]);
```

For definitions and conventions regarding global and local coordinates, see "Global and Local Coordinate Systems".

Use rangeangle to determine the range and angle between the antenna and the target.

```
[tgtrng,tgtang] = rangeangle(htgtplat.InitialPosition,...
htxplat.InitialPosition);
```

See "Motion Modeling in Phased Array Systems" for more details on modeling motion.

Modeling the Transmitter

To model the transmitter specifications, use phased. Transmitter. A key parameter in modeling a transmitter is the peak transmit power. To determine the peak transmit power, assume that the desired probability of detection is 0.9 and the maximum tolerable false-alarm probability is 10^{-6} . Assume that the ten rectangular pulses are noncoherently integrated at the receiver. You can use albersheim to determine the required signal-to-noise ratio (SNR).

```
Pd = 0.9;
Pfa = 1e-6;
numpulses = 10;
SNR = albersheim(Pd,Pfa,10);
```

The required SNR is approximately 5 dB. Assume you want to set the peak transmit power in order to achieve the required SNR for your target at a range of up to 15 kM. Assume that the transmitter has a 20 dB gain. You can use radaregpow to determine the required peak transmit power.

```
maxrange = 1.5e4;
lambda = physconst('LightSpeed')/4e9;
tau = hwav.PulseWidth;
Pt = radareqpow(lambda,maxrange,SNR,tau,'RCS',0.5,'Gain',20);
```

The required peak transmit power is approximately 45 kilowatts. To be conservative, use a peak power of 50 kilowatts in modeling your transmitter. To maintain a constant phase in the pulse waveforms, set the CoherentOnTransmit property to true. Because you are operating the transmitter in a monostatic (transmit-receive) mode, set the InUseOutputPort property to true to keep a record of the transmitter status.

```
htx = phased.Transmitter('PeakPower',50e3,'Gain',20,...
    'LossFactor',0,'InUseOutputPort',true,...
    'CoherentOnTransmit', true);
```

See "Transmitter" for more examples on modeling transmitters and "Radar Equation" for examples involving the radar equation.

Modeling Waveform Radiation and Collection

To model waveform radiation from the array, use phased.Radiator. To model narrowband signal collection at the array, use phased.Collector. For wideband signal collection, use phased.WidebandCollector.

In this example, the pulse satisfies the narrowband assumption around the carrier frequency of 4 GHz. For the value of the Sensor property, use the handle for the isotropic antenna. In phased.Collector, setting the Wavefront property to 'Plane' assumes the waveform incident on the antenna is a plane wave.

```
hrad = phased.Radiator('Sensor',hant,...
    'PropagationSpeed', physconst('LightSpeed'),...
    'OperatingFrequency',4e9);
hcol = phased.Collector('Sensor',hant,...
    'PropagationSpeed',physconst('LightSpeed'),...
    'Wavefront', 'Plane', 'OperatingFrequency', 4e9);
```

Modeling the Receiver

To model the receiver in "Radar Scenario" on page 5-3, use phased.ReceiverPreamp. In the receiver, you specify the noise figure and reference temperature, which are key contributors to the internal noise of your system. In this example, set the noise figure to 2 dB and the reference temperature to 290 degrees kelvin. Seed the random number generator for reproducible results.

```
hrec = phased.ReceiverPreamp('Gain',20,'NoiseFigure',2,...
    'ReferenceTemperature',290,'SampleRate',1e6,...
    'EnableInputPort',true,'SeedSource','Property','Seed',1e3);
```

See "Receiver Preamp" for more details.

Modeling the Propagation Environment

To model the propagation environment in "Radar Scenario" on page 5-3, use phased.FreeSpace. You can model one-way and two-propagation by setting the TwoWayPropagation property. In this example, set this property to false to model one-way propagation.

```
hspace = phased.FreeSpace(...
    'PropagationSpeed',physconst('LightSpeed'),...
    'OperatingFrequency',4e9,'TwoWayPropagation',false,...
'SampleRate',1e6);
```

See "Free Space Path Loss" for more details.

Implementing the Basic Radar Model

Having parameterized all the necessary components for the model outlined in "Radar Scenario" on page 5-3, you are ready to generate the pulses, propagate the pulses to and from the target, and collect the echoes.

The following code prepares for the main simulation loop.

```
% Time step between pulses
T = 1/hwav.PRF;
% Get antenna position
txpos = htxplat.InitialPosition;
% Allocate array for received echoes
rxsig = zeros(hwav.SampleRate*T,numpulses);
```

You can execute the main simulation loop with the following code:

```
for n = 1:numpulses
    % Update the target position
    tgtpos = step(htgtplat,T);
    % Get the range and angle to the target
    [tgtrng,tgtang] = rangeangle(tgtpos,txpos);
    % Generate the pulse
    sig = step(hwav);
    % Transmit the pulse. Output transmitter status
    [sig,txstatus] = step(htx,sig);
    % Radiate the pulse toward the target
    sig = step(hrad,sig,tgtang);
```

```
% Propagate the pulse to the target in free space
    sig = step(hspace,sig,txpos,tgtpos);
    % Reflect the pulse off the target
    sig = step(htgt,sig);
    % Propagate the echo to the antenna in free space
    sig = step(hspace,sig,tgtpos,txpos);
    % Collect the echo from the incident angle at the antenna
    sig = step(hcol,sig,tgtang);
    % Receive the echo at the antenna when not transmitting
    rxsig(:,n) = step(hrec,sig,~txstatus);
end
```

Noncoherently integrate the received echoes, create a vector of range gates, and plot the result. The red vertical line on the plot marks the range of the target.

```
rxsig = pulsint(rxsig, 'noncoherent');
t = unigrid(0,1/hrec.SampleRate,T,'[)');
rangegates = (physconst('LightSpeed')*t)/2;
plot(rangegates,rxsig); hold on;
xlabel('Meters'); ylabel('Power');
ylim = get(gca, 'YLim');
plot([tgtrng,tgtrng],[0 ylim(2)],'r');
```

